

#1. Complete the table to determine the amount of money P that should be invested at $r = 8\%$ compounded continuously to produce a final balance of \$200,000 in t years. (round to nearest dollar)

| | | | | | | |
|---|----------|---------|---------|---------|--------|--------|
| t | 1 | 10 | 20 | 30 | 40 | 50 |
| P | \$184623 | \$99866 | \$40379 | \$18144 | \$8152 | \$3663 |

$$A = Pe^{rt}$$

$$200000 = Pe^{.08t} \quad P = \frac{200000}{e^{.08t}} \quad (\text{put in calc Y1=, use table listing})$$

#2. Complete the table to determine the amount of money P that should be invested at $r = 10\%$ compounded monthly to produce a final balance of \$200,000 in t years. (round to nearest dollar)

| | | | | | | |
|---|----------|---------|---------|---------|--------|--------|
| t | 1 | 10 | 20 | 30 | 40 | 50 |
| P | \$181042 | \$73881 | \$27292 | \$10082 | \$3724 | \$1376 |

$$A = P\left(1 + \frac{r}{n}\right)^{nt} \quad n=12$$

$$200000 = P\left(1 + \frac{.10}{12}\right)^{12t} \quad P = \frac{200000}{\left(1 + \frac{.10}{12}\right)^{12t}} \quad (\text{put in calc Y1=, use table listing})$$

#3. Write the exponential equation in logarithmic form: $4^3 = 64$ $\log_4 64 = 3$

#4. Evaluate the expression without using a calculator: $\log_6 216$ $\log_6 216 = x$
 $6^x = 216$ $6 \cdot 6 \cdot 6 = 216$
 $x = 3$

#5. Evaluate the logarithm using the change of base formula (round to 3 decimal places): $\log_{12} 200$

$$\log_{12} 200 = \frac{\ln 200}{\ln 12} = \boxed{2.132}$$

#6. Rewrite the expression as a sum, difference, and/or multiple of logarithms: $\log_{10} \frac{5\sqrt{y}}{x^2}$

$$\log_{10} 5\sqrt{y} - \log_{10} x^2$$

$$\log_{10} 5 + \log_{10} \sqrt{y} - \log_{10} x^2 \rightarrow \log_{10} 5 + \log_{10} y^{1/2} - \log_{10} x^2$$
 $\log_{10} 5 + \frac{1}{2} \log_{10} y - 2 \log_{10} x$

#7. Write the expression as the logarithm of a single quantity: $3[\ln x - 2 \ln(x^2 + 1)] + 2 \ln 5$

$$3 \ln x - 6 \ln(x^2 + 1) + 2 \ln 5$$

$$\ln x^3 - \ln(x^2 + 1)^6 + \ln 5^2$$

$$\ln x^3 - \ln(x^2 + 1)^6 + \ln 25$$
 $\ln \left(\frac{25x^3}{(x^2+1)^6} \right)$

#8. Solve for x: $8^x = 512$
 $8 \cdot 8 \cdot 8 = 512$ - or - $\log_8(8^x) = \log_8 512$
 $x = \log_8 512 = \frac{\ln 512}{\ln 8} = 3$
 $x = 3$

#9. Solve for x: $\log_7 x = 4$
 write in exponential form: $7^4 = x$
 $x = 2401$

#10. The population of a town is modeled by $P = 12,620 e^{0.0118t}$ where $t = 0$ represents the year 2000. According to this model, when will the population reach 17,000?

$17000 = 12620 e^{0.0118t}$
 $\frac{17000}{12620} = e^{0.0118t}$
 $\ln\left(\frac{17000}{12620}\right) = \ln(e^{0.0118t})$
 $\ln\left(\frac{17000}{12620}\right) = 0.0118t$
 $t = \frac{\ln\left(\frac{17000}{12620}\right)}{0.0118} = 252.7$
 $t = 252 + 7000$
 2025

#11. A deposit of \$10,000 is made in a savings account for which the interest is compounded continuously. The balance will double in 12 years.

(a) What is the annual interest rate for this account?

$r = 5.78\%$

$A = Pe^{rt}$
 $20000 = 10000 e^{12r}$
 $\frac{20000}{10000} = e^{12r}$
 $2 = e^{12r}$
 $\ln 2 = 12r$
 $r = \frac{\ln 2}{12}$
 $r = .05776$

(b) Find the balance after 1 year.

$A = 10000 e^{0.0578(1)} = \10595.03

(c) The effective yield of a savings plan is the percent increase in the balance after 1 year. Find the effective yield.

$\$10595.03 - \$10000 = \$595.03$ gain
 $\frac{595.03}{10000} = .0595$
 5.95%

#1.

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#3. $\log_4 64 = 3$ #4. 3 #5. 2.132 #6. $\log_{10} 5 + \frac{1}{2} \log_{10} 2 - 2 \log_{10} x$

#7. $\ln \left(\frac{25x^2}{(x^2+1)^6} \right)$ #8. 3 #9. 2401 #10. in 2025

#11. (a) 5.78% (b) \$10595.03 (c) 5.95%

Honors Algebra 3-4
Chapter 3 Pre-Quiz Review

Name _____
Period _____

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#11. A deposit of \$10,000 is made in a savings account for which the interest is compounded continuously. The balance will double in 12 years.

- (a) What is the annual interest rate for this account?
- (b) Find the balance after 1 year.
- (c) The effective yield of a savings plan is the percent increase in the balance after 1 year. Find the effective yield.

#11. (a) 5.78% (b) \$10595.03 (c) 5.95%

#7. $\ln \left(\frac{25x^2}{x^2+1} \right)$

#8. 3

#9. 2401

#10. $\ln 2025$

#3. $\log_4 64 = 3$

#4. 3

#5. 2.132

#6. $\log_{10} 5 + \frac{1}{2} \log_{10} 7 - 2 \log_{10} x$

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ANSWERS: