

1. Solve for  $x$  if 
$$\begin{bmatrix} 10 & -5 & 0 \\ x/3 & 15 & 17 \\ -2 & 4 & -3 \end{bmatrix} = \begin{bmatrix} 10 & -5 & 0 \\ 2x-10 & 15 & 17 \\ -2 & 4 & -3 \end{bmatrix}$$

2. Solve for  $x$ : (show work) 
$$\begin{bmatrix} -2 & -1 & 0 \\ x & 3 & 2 \end{bmatrix} \begin{bmatrix} 1 & -4 \\ 0 & 2 \\ 3 & 1 \end{bmatrix} = \begin{bmatrix} -2 & 6 \\ 3 & 20 \end{bmatrix}$$

3. A small corporation borrowed \$500,000 to build a new office building. Some of the money was borrowed at 9% interest, some at 10% interest, and some at 12% interest. How much was borrowed at each rate if the annual interest was \$52,000 and the amount borrowed at 10% was 2.5 times the amount borrowed at 9%?

4. **Without a calculator**, solve the systems of equations by writing an augmented matrix and using Gauss-Jordan elimination (show all steps).

a) 
$$\begin{cases} -3x + 2y = 0 \\ x - y = -1 \end{cases}$$

b) 
$$\begin{cases} 4x + 3y = 5 \\ 3x + 2y = 4 \end{cases}$$

5. Let  $A = \begin{bmatrix} 2 & 3 \\ -1 & 1 \\ 0 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & -1 \\ 0 & 2 \\ 2 & 0 \end{bmatrix}$  **Without a calculator**, solve for  $X$  if  $3X - 2A = B$  (show work)

6. If  $A = \begin{bmatrix} 2 & 1 \\ -1 & 3 \end{bmatrix}$ , find  $A^{-1}$

7. Solve the system of equations by using Cramer's Rule.

$$\begin{cases} 2x - y + z = 5 \\ 3x + 2y + 5z = 18 \\ x - y + 4z = 5 \end{cases}$$

8. Let  $A = \begin{bmatrix} 1 & 1 & 1 \\ 2 & -1 & 1 \\ -1 & 1 & 3 \end{bmatrix}$  and  $B = \begin{bmatrix} 6 \\ -2 \\ 0 \end{bmatrix}$  Use a matrix inverse to solve for  $X$  if  $AX = B$  (show work)

9. Evaluate using the method of expansion by minors and cofactors:

$$\begin{vmatrix} 0 & 2 & 1 \\ 3 & -1 & 2 \\ 4 & 0 & 1 \end{vmatrix}$$

10. Use a determinant to find the area of a triangle with vertices at  $(-1, -4)$ ,  $(3, -2)$ ,  $(6, 8)$

11. Set up and use the determinant of a matrix to determine if  $(2,4)$ ,  $(-3,-6)$ , and  $(1,-2)$  are collinear.

12. Find the value of  $x$  that makes the triangle formed by the three ordered pairs have an area of 12.  
 $(2,3), (1,0), (-1,x)$